

CHAPTER FIVE

RTL NOR Gate

Digital Electronics.

Introduction

- RTL Inverter: discussed in Ch.4
- RTL NOR gate
- RTL NAND gate
- RTL OR gate
- RTL AND gate

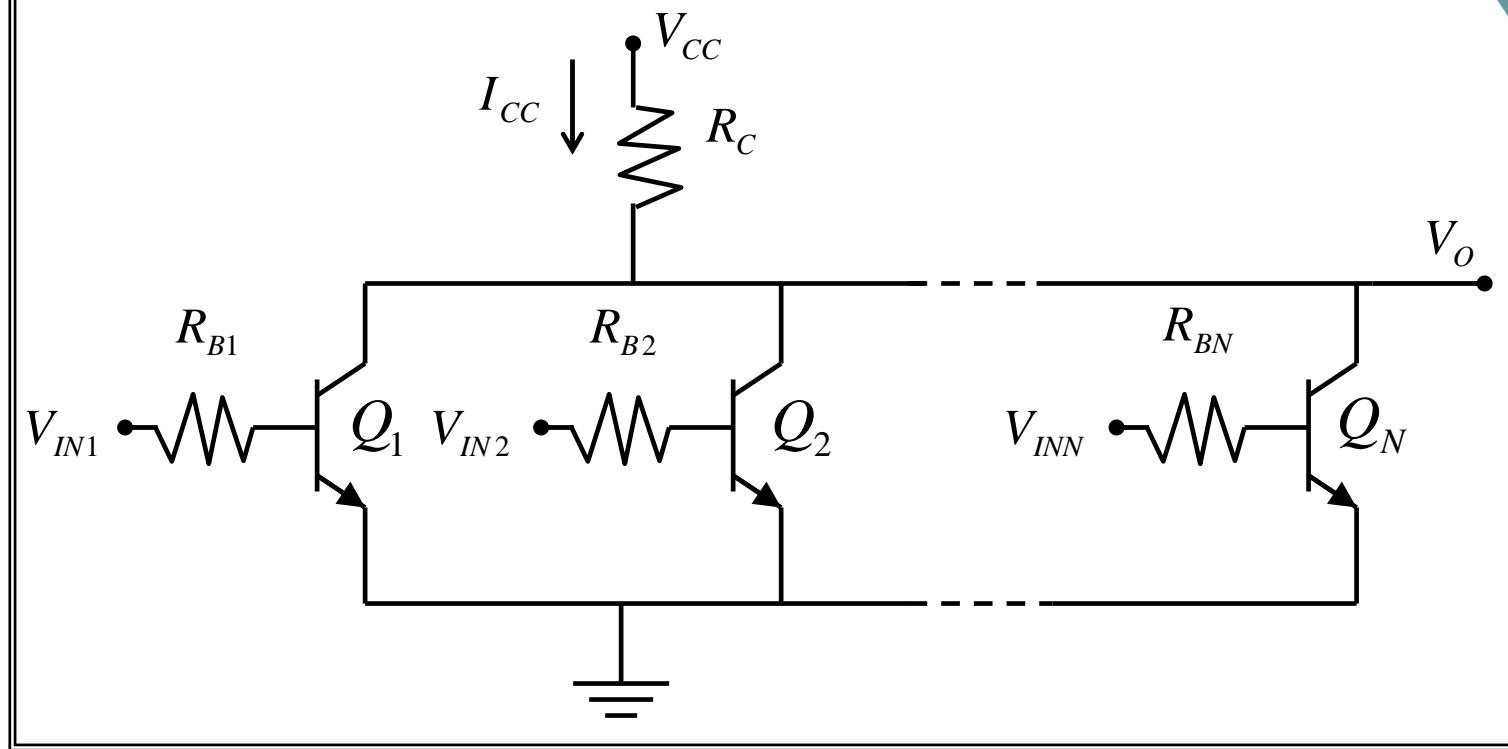


Basic RTL NOR Gate

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$$I_{CC} = \sum_{n=1}^N I_{Cn}$$



$$V_O = V_{CC} - I_{CC}R_C$$

If all inputs are less than V_{BE} (FA)

$\Rightarrow V_O = V_{CC}$
High

If at least one input is greater than V_{IH}

$\Rightarrow V_O = V_{CE}(\text{sat})$
Low

Basic RTL NAND Gate

Assuming $\beta_F \gg 1$, I_B is negligible to I_C

$$I_{CC} = I_{C1} \cong I_{E1} \cong I_{E2}$$

$$V_o = V_{cc} - I_{cc} R_c$$

If at least one input less than $V_{BE}(FA)$, then the corresponding Q is off. i.e. $I_{CC}=0$

$$V_{OH} = V_{CC}$$

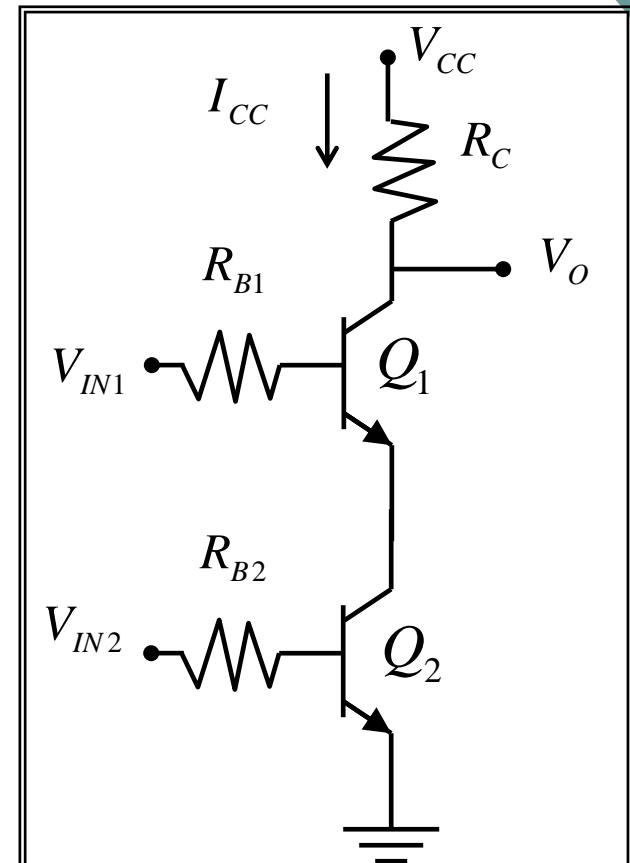
$$V_Q = V_{CE}(sat)$$

Q_2 starts conducting (ON) if $V_{IN2} > V_{BE2}$ (FA)

Q_1 starts conducting (ON) if $V_{IN1} > V_{BE1}(\text{FA}) + V_{CE2}(\text{sat})$

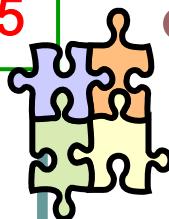
If both Q_1 and Q_2 are saturated

$$V_o = 2V_{CE}(\text{sat})$$



V_o starts decreasing below V_{cc}

Multi-Input RTL NAND Gate



$$V_{OH} = V_{CC} - I_{CC}R_C$$

$$V_{OL} = \sum_{n=1}^N V_{CEn}(\text{sat})$$

Note: Number of inputs of an RTL NAND is limited

Example

Determine the maximum **fan-in** for basic RTL NAND gate, assuming $V_{CE}(\text{sat})=0.2\text{V}$, $V_{BE}(\text{FA})=0.7\text{V}$

Solution

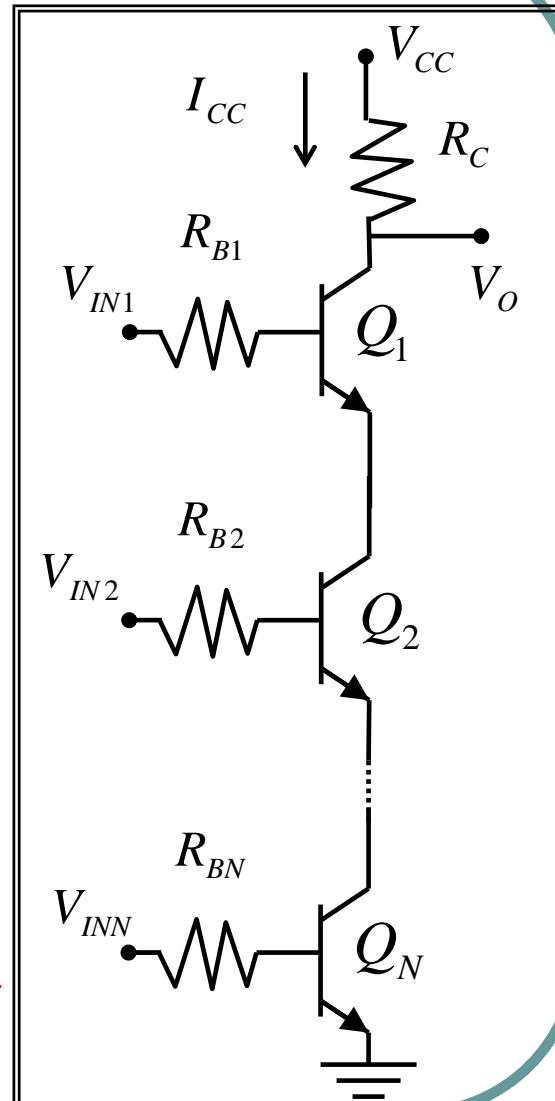
$$\text{MUST } N_{ML} = V_{IL} - V_{OL} > 0 \quad N_{MH} = V_{OH} - V_{IH} > 0$$

$$V_{IL} > V_{OL} \Rightarrow 0.7 > N \times V_{CE}(\text{sat}) \quad \rightarrow$$

$$N < \frac{0.7}{0.2} = 3.5 \Rightarrow N = 3$$

Always valid

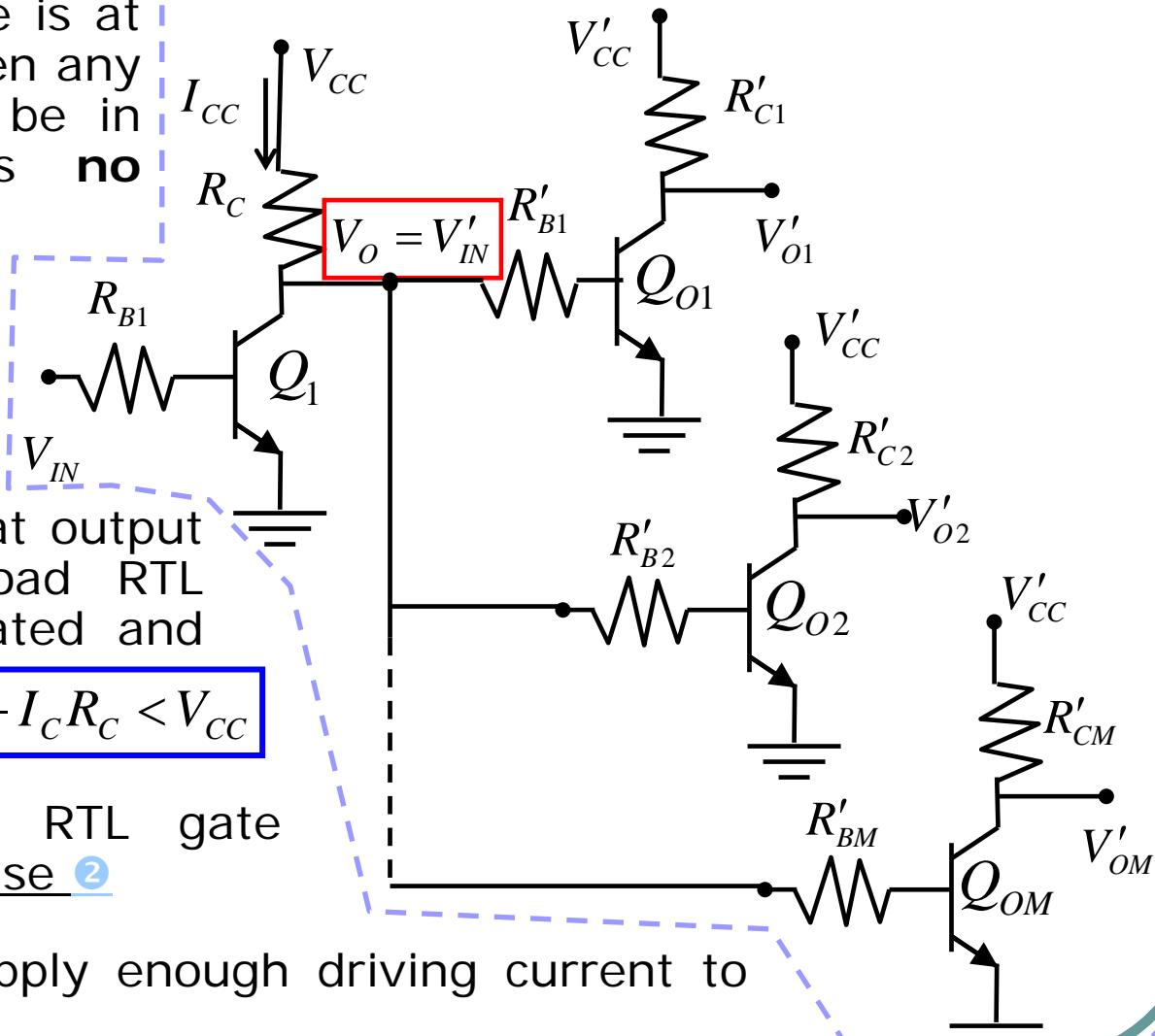
$$V_{OH} > V_{IH} \Rightarrow V_{CC} > V_{BE}(\text{FA}) \quad \checkmark$$



RTL Fan-Out

1 When an RTL gate is at output **low** state, then any load RTL gate will be in cut-off and draws **no** current

$$V_{OL} = V_{CE}(\text{sat}) \\ = V'_{IN} < V_{BE}(\text{FA})$$



2 When an RTL gate is at output **high** state, then all load RTL gates will be in saturated and draw current

$$V_{OH} = V_{CC} - I_C R_C < V_{CC}$$

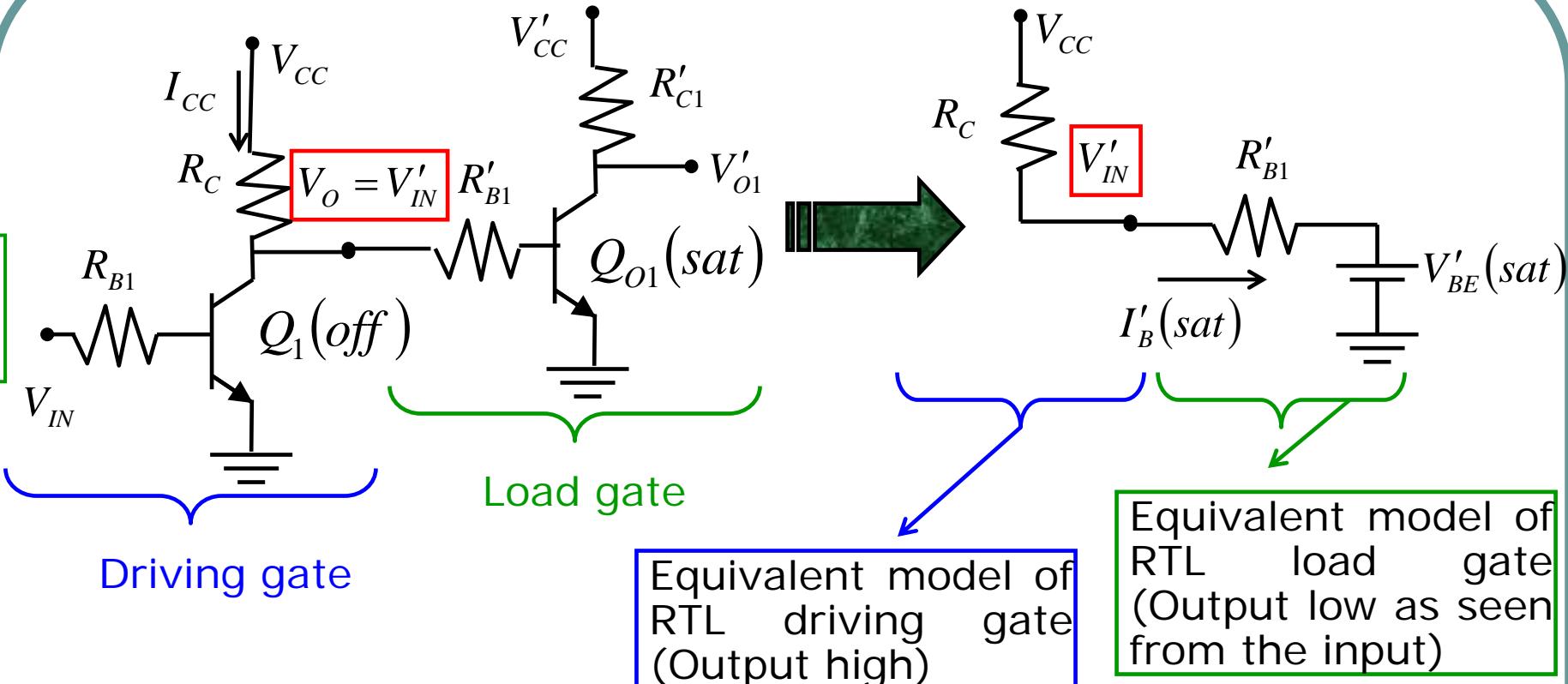
3 Maximum fan-out of RTL gate therefore depends on case 2

4 Driving gate must supply enough driving current to saturate all load gates

RTL Fan-Out

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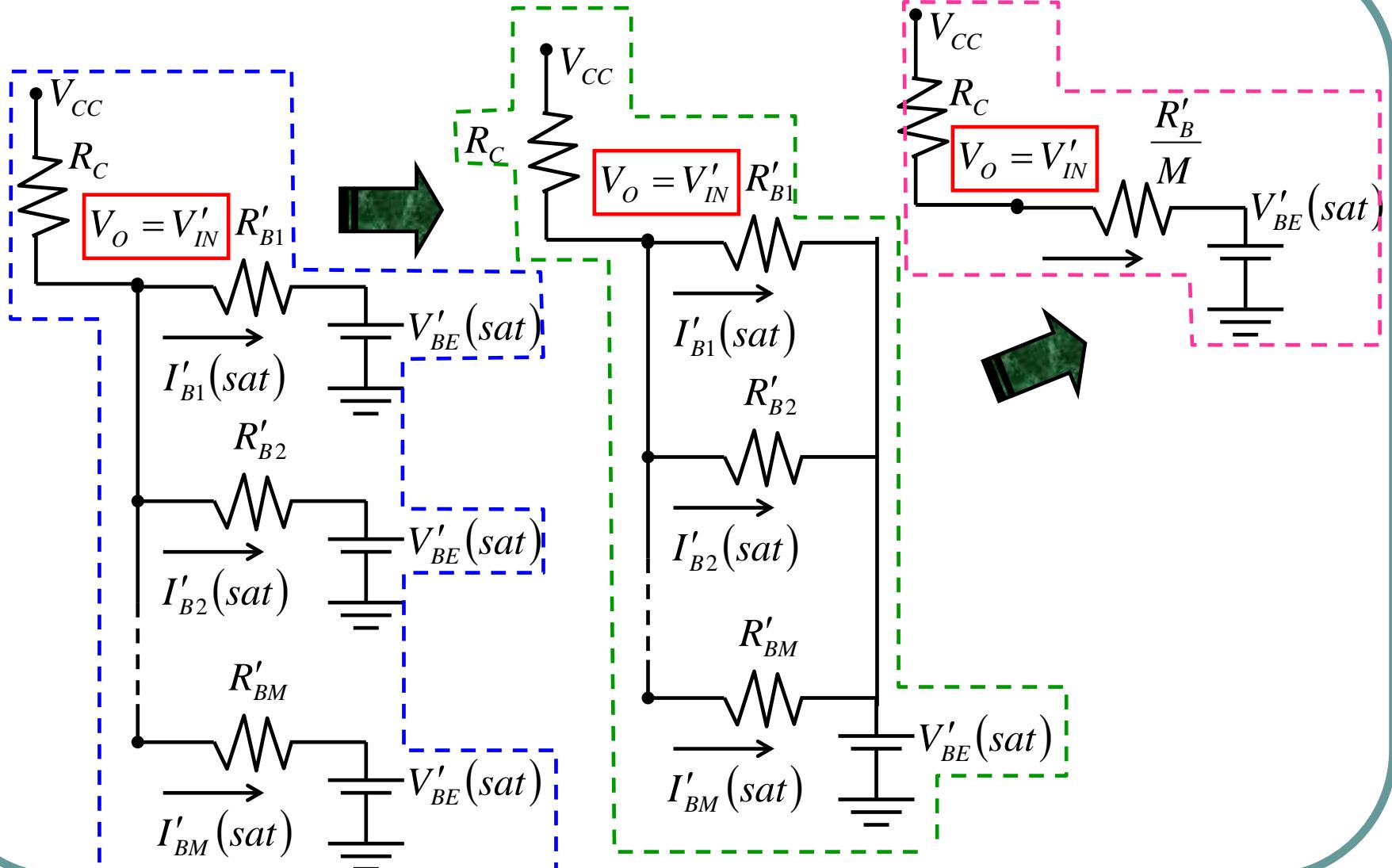


RTI Fan-Out

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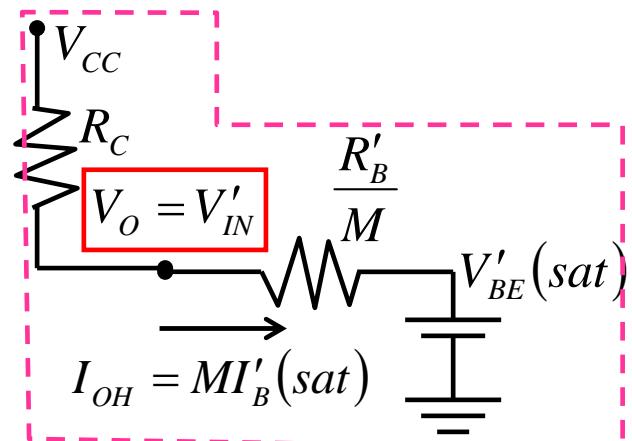


RTL Fan-Out

$$\frac{V_{CC} - V_o}{R_C} = \frac{V_o - V_{BE}(\text{sat})}{R'_B/M}$$

$$M = \frac{(V_{CC} - V_o)/R_C}{(V_o - V_{BE}(\text{sat}))/R'_B} \quad \star$$

$$M = \frac{I_{OH}}{I_{IH}}$$



1 As M increases, the collector current of the driving gate increases, i.e. V_{OH} decreases. V_{OH} should be large enough to saturate all load gates

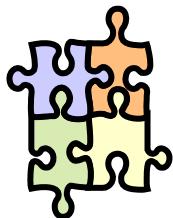
$$V_{OH}(\text{min}) = V_{IH} = \frac{V_{CC} - V_{CE}(\text{sat})}{\beta_F R'_C} R'_B + V'_{BE}(\text{sat}) \quad \star \star \quad (\text{Proved in p. 10 of CH.4})$$

2 Now, substituting $V_{OH}(\text{min})$ ($\star \star$) as V_o in (\star) gives the maximum fan-out

RTL Fan-Out

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• Example

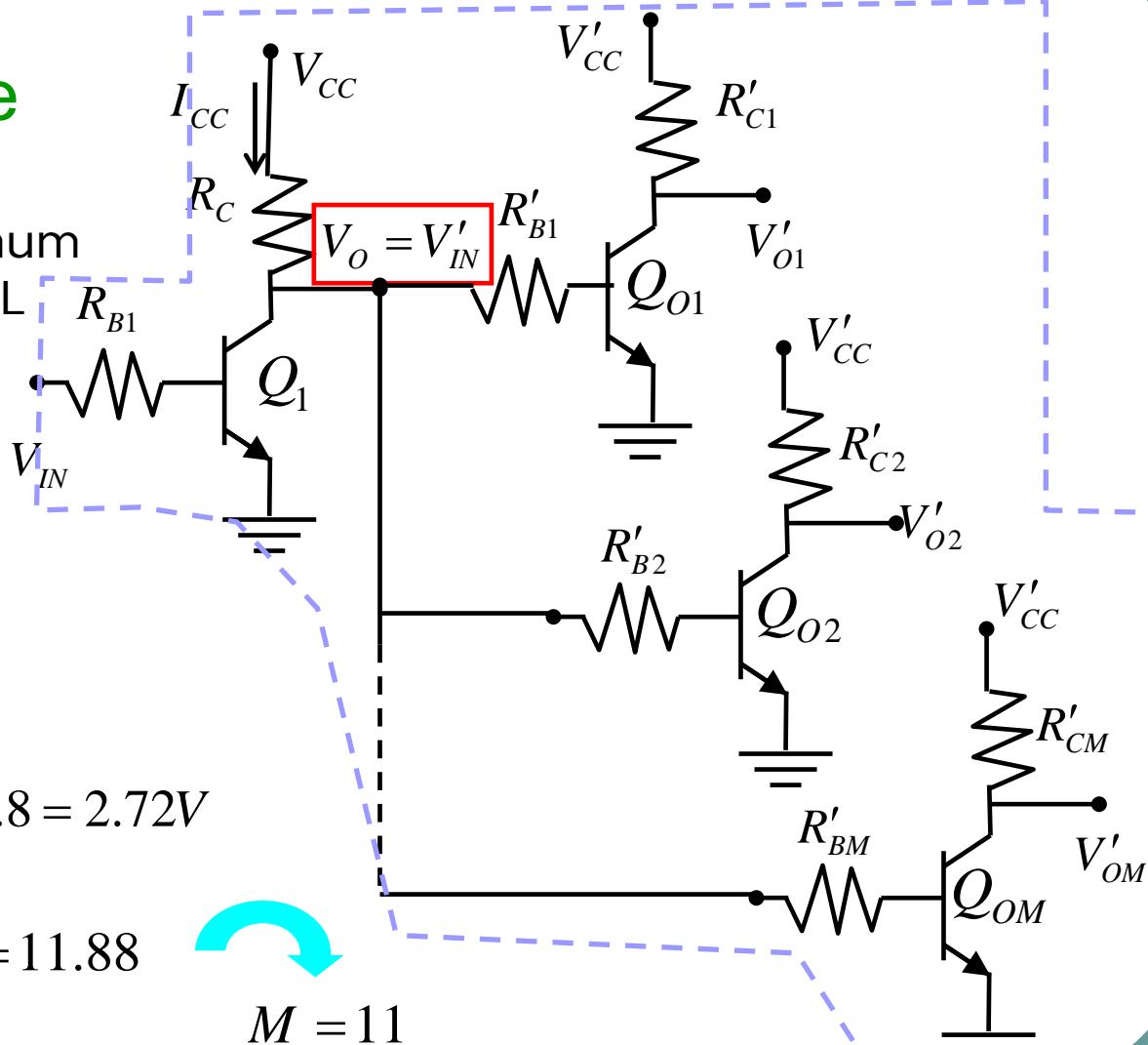
Determine the maximum **fan-out** for driving RTL gate, assuming $V_{CE}(\text{sat})=0.2\text{V}$, $V_{BE}(\text{sat})=0.8\text{V}$, $\beta_F=25$, $V_{CC}=5\text{V}$, $R_C=1\text{k}\Omega$, $R_B=10\text{k}\Omega$

• Solution

$$V_{OH}(\text{min}) = \frac{5-0.2}{25} \times 10 + 0.8 = 2.72\text{V}$$

$$\text{But } M = \frac{(5-2.72)/1}{(2.72-0.8)/10} = 11.88$$

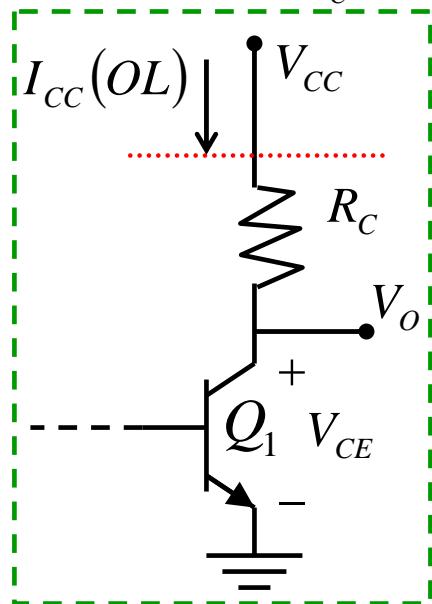
$$M = 11$$



RTL Power-Dissipation

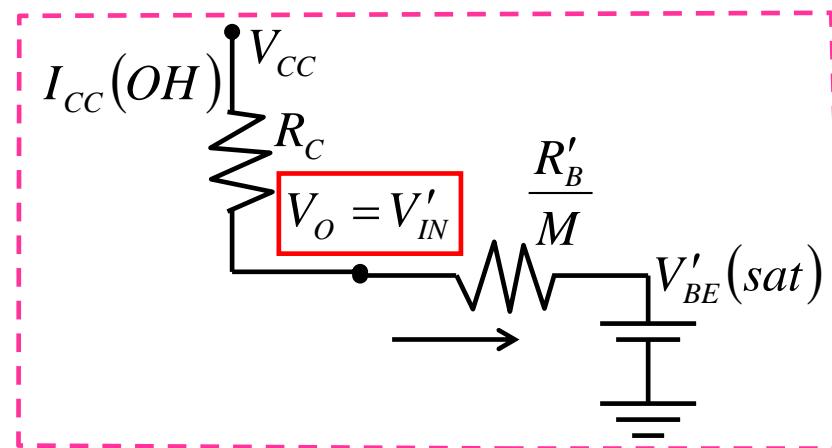
Output low supplied current
 $= I_{CC}(OL)$

$$I_{CC}(OL) = \frac{V_{CC} - V_{CE}(sat)}{R_C}$$



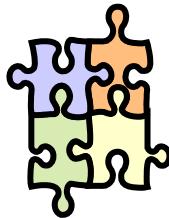
Output high supplied current
 assuming M-load gates
 $= I_{CC}(OH)$

$$I_{CC}(OH) = \frac{V_{CC} - V_{BE}(sat)}{R_C + \frac{R'_B}{M}}$$



$$P_{CC}(avg) = V_{CC} \left(\frac{I_{CC}(OH) + I_{CC}(OL)}{2} \right)$$

RTL Power-Dissipation



• Example

Determine the average dissipated power for

- A. No load
- B. Fan-out of 1

Assuming $V_{CE}(\text{sat})=0.2\text{V}$, $V_{BE}(\text{sat})=0.8\text{V}$, $\beta_F=25$, $V_{CC}=5\text{V}$, $R_C=1\text{k}\Omega$, $R_B=10\text{k}\Omega$

• Solution

A. No load:

$$I_{CC}(OL) = \frac{V_{CC} - V_{CE}(\text{sat})}{R_C}$$
$$= \frac{5 - 0.2}{1} = 4.8\text{mA}$$

$$I_{CC}(OH) = 0\text{mA}$$

}

$$P_{CC}(\text{avg}) = 5 \left(\frac{4.8}{2} \right) = 12\text{mW}$$

B. $M=1$:

$$I_{CC}(OL) = \frac{V_{CC} - V_{CE}(\text{sat})}{R_C}$$
$$= \frac{5 - 0.2}{1} = 4.8\text{mA}$$

$$I_{CC}(OH) = \frac{V_{CC} - V_{BE}(\text{sat})}{R_C + \frac{R'_B}{M}}$$
$$= \frac{5 - 0.8}{1 + 10} = 0.382\text{mA}$$

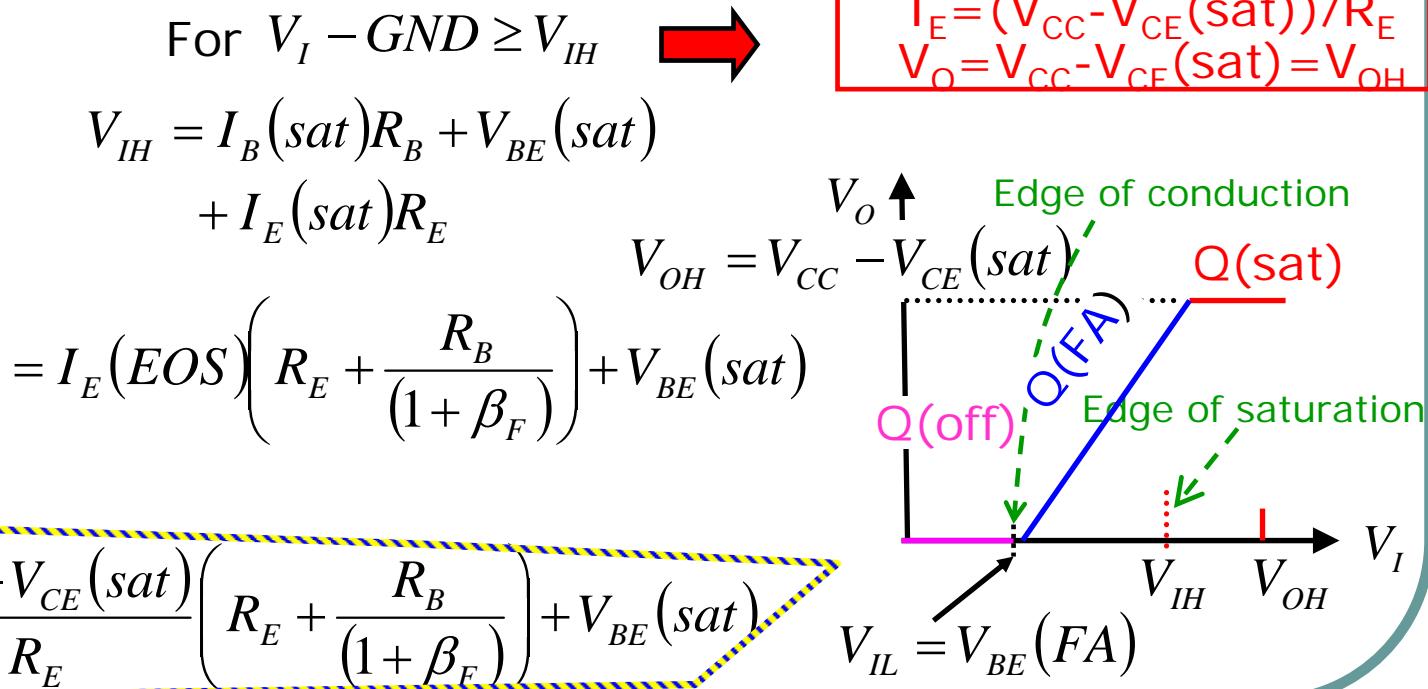
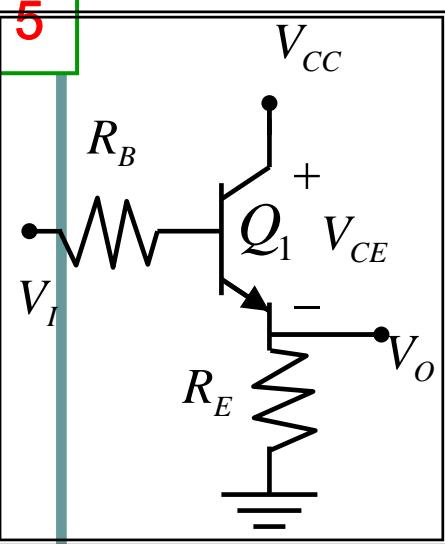
$$P_{CC}(\text{avg}) = 5 \left(\frac{4.8 + 0.382}{2} \right)$$
$$= 12.96\text{mW}$$

Basic RTL Non-Inverter (Emitter Follower in)

- Voltage-Transfer Characteristics

For $V_I - GND < V_{BE}(FA)$ $\rightarrow I_B = 0, I_C = 0, V_O = 0 = V_{OL}$

For $V_I - GND \geq V_{BE}(FA)$ $\rightarrow I_B = (V_I - V_{BE}(FA)) / (R_B + (1 + \beta_F)R_E), V_O = R_E(V_I - V_{BE}(FA)) / (R_B / (1 + \beta_F) + R_E)$

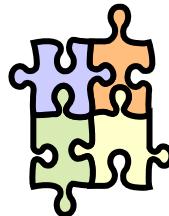


$$V_{IH} = \frac{V_{CC} - V_{CE(sat)}}{R_E} \left(R_E + \frac{R_B}{(1 + \beta_F)} \right) + V_{BE}(sat)$$

$$V_{IL} = V_{BE}(FA)$$

BJT Non-Inverter (Basic RTL Non-Inverter)

- **Example**



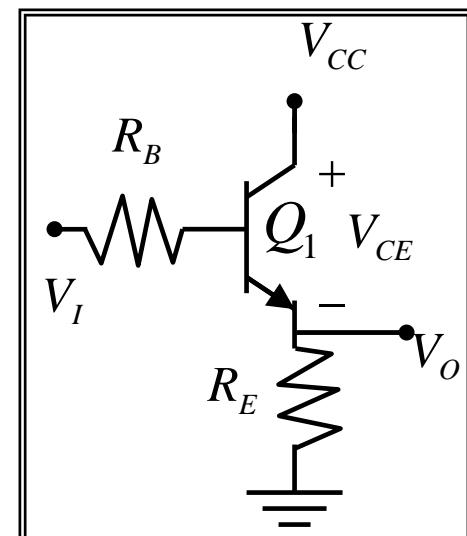
Assume $V_{CC} = 5$ V, $R_E = 1\text{k}\Omega$, $R_B = 10\text{k}\Omega$, $\beta_F = 25$;
 $V_{CE(\text{sat})} = 0.2$ V, $V_{BE(\text{sat})} = 0.8$ V, $V_{BE(\text{FA})} = 0.7$ V,

Determine the VTC parameters

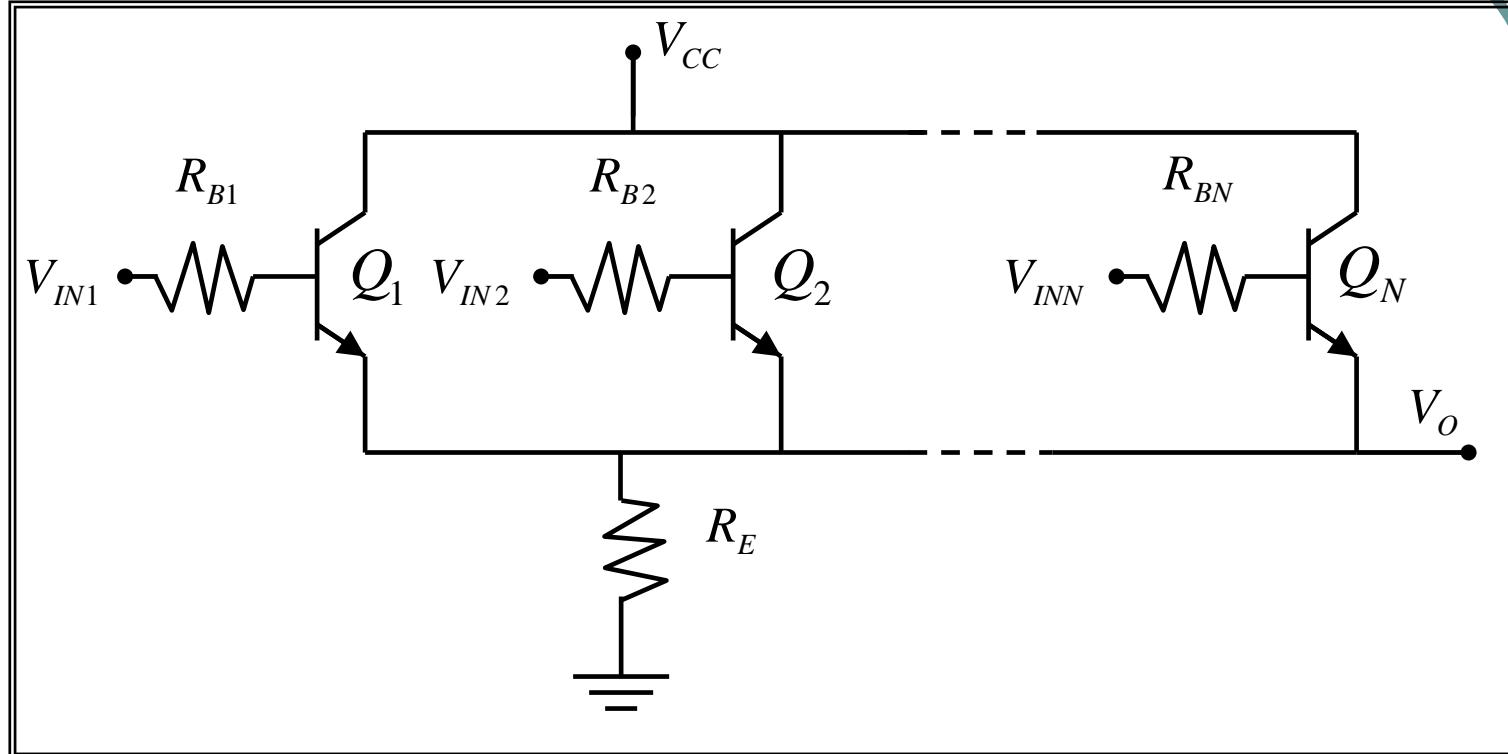
- **Solution**

$$V_{IL} = 0.7 \text{ V}, \quad V_{OL} = 0.0 \text{ V},$$

$$V_{IH} = 7.45 \text{ V}, \quad V_{OH} = 4.8 \text{ V},$$



Basic RTL OR Gate



If all inputs are less than $V_{BE}(\text{FA})$ $\rightarrow V_o = 0$ Low

If at least one input is greater than V_{IH} $\rightarrow V_o = V_{CC} - V_{CE}(\text{sat})$ High